

# Projectiles (Horizontal Launch)

- Projectile - Any object that is thrown, kicked, etc., while in mid air (after release)
- in free fall
  - only influenced by gravity (the only force)

## Examples

Footballs after being thrown

Frog after a jump (in mid air)

High jumper after leaving ground

## Not Examples

Airplane

Bird

Rocket

Gliders

Skydiver (parachute open)

Hang Glider

For projectiles,

①  $\vec{a}_y = 9.8 \text{ m/s}^2$  [down], on Earth (constant)

acceleration in  
y-direction  
only

②  $\vec{v}_x$  is constant!!

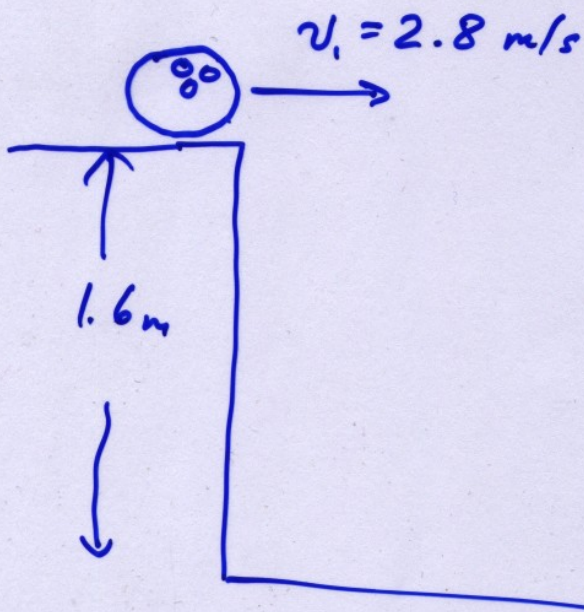
velocity in x-direction only.



- ③ Analyse the x and y directions separately! (Time is common to both directions)

Example: Selma's bowling ball rolls off her 1.6 m high counter with an initial horizontal speed of 2.8 m/s. Determine

- (a) how long it takes for the ball to reach the floor (called "time of flight").  
(b) the impact velocity of the ball.



(a) y-direction

$$\vec{a}_d = -1.6 \text{ m}$$

$$\vec{a} = -9.8 \text{ m/s}^2$$

$$\vec{v}_i = 0$$

$$\Delta t = ?$$

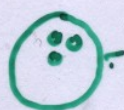
$$\vec{a}_d = \vec{v}_i \Delta t + \frac{1}{2} \vec{a} \Delta t^2$$

$$-1.6 = 0 + \frac{1}{2} (-9.8) \Delta t^2$$

$$\Delta t = 0.57 \text{ s}$$



(b)



Galileo showed that  
all projectiles follow  
a parabolic  
trajectory

$$v_{x2} = v_{x1} = 2.8 \text{ m/s}$$

y-direction:

$$v_{y1} = 0$$

$$a_y = -9.8 \text{ m/s}^2$$

$$v_{y2} = ?$$

$$\Delta t = 0.57 \text{ s}$$

$$\vec{v}_2 = \vec{v}_1 + \vec{a} \Delta t$$

$$= 0 + (-9.8)(0.57)$$

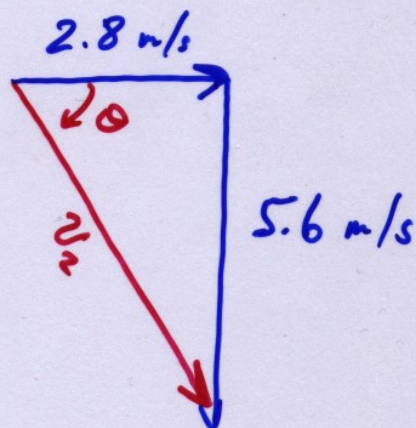
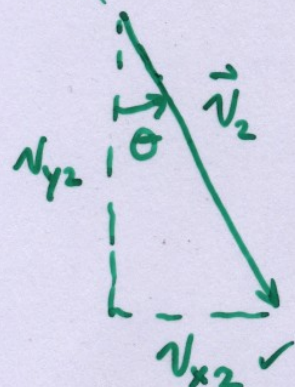
$$= -5.6 \text{ m/s}$$

$$\vec{v}_2^2 = (2.8)^2 + (5.6)^2$$

$$v_2 = 6.3 \text{ m/s}$$

$$\vec{v}_2 = 6.3 \text{ m/s}$$

$$[E 63.4^\circ S]$$



$$\tan \theta = \frac{5.6}{2.8}$$

$$\theta = 63.4^\circ$$